

Lab Worksheet for September 28, 2021

Practice with Implicit Differentiation.

1. Consider the shape formed by the equation $x^2 - y^2 = 4$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(2, 0)$.

2. Consider the shape formed by the equation $x^4y - xy^3 = -2$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(-1, -1)$.

3. Consider the shape formed by the equation $x^2y^2 + 5xy = 14$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(2, 1)$.

4. Consider the shape formed by the equation $\tan(xy) = y$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(\frac{\pi}{4}, 1)$.

5. Consider the shape formed by the equation $xy^2 + \sin(\pi y) - 2x^2 = 10$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(2, -3)$.

6. Consider the shape formed by the equation $\frac{x}{y} + 5x - 7 = -\frac{3}{4}y$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(1, 2)$.

7. Consider the shape formed by the equation $xy + \sin(x) = 1$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(\frac{\pi}{2}, 0)$.

8. Consider the shape formed by the equation $6x^2 + 3y^2 = 12$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(0, 2)$.

9. Consider the shape formed by the equation $xy - \cos(y) = 1$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(0, -\pi)$.

10. Consider the shape formed by the equation $x^4 + y^2 = 1$

(a) Write down the formula for the slope of the tangent line to this shape at a point (x, y) on this shape.

(b) Find the slope of the tangent line to this shape at the point $(0, 1)$.